

2014 HIGHER SCHOOL CERTIFICATE EXAMINATION

**Mathematics General 2****Section II****75 marks****Attempt Questions 26–30****Allow about 1 hour and 55 minutes  
for this section**

Answer the questions in the spaces  
provided.

Your responses should include  
relevant mathematical reasoning  
and/or calculations.

Extra writing space is provided on  
pages 33 and 34. If you use this space,  
clearly indicate which question you  
are answering.

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**Please turn over**

**Question 26** (15 marks)

$$4x(7+x^4-x^2)$$

(a) Expand  $4x(7x^4 - x^2)$ .

1

~~4x(7x^4-x^2)~~  $4x(7+x^4-x^2)$

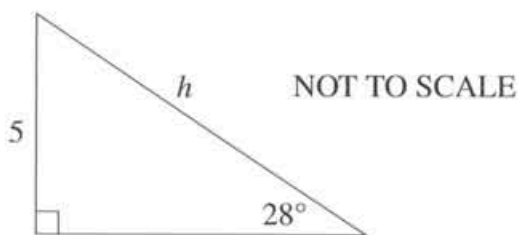
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.....

(b) Calculate the value of  $h$  correct to two decimal places.

2



~~tan 28 = 5/h~~ ~~h = 5/tan 28~~

~~h = 10.17~~

$\frac{5}{28} \times 100 = 17.85$

$h = 17.85$

.....

.....

.....

(c) Solve the equation  $\frac{5x+1}{3} - 4 = 5 - 7x$ .

3

$\frac{5x+1}{3} - 4 = -2 + 5 - 7x$

$\frac{5x+1}{3} = -4$

.....

.....

.....

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.....

.....

Question 26 continues on page 15

Question 26 (continued)

- (d) Solve these simultaneous equations to find the values of  $x$  and  $y$ . 3

$$y = 2x + 1$$

$$x - 2y - 4 = 0$$

*Answer*

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$y = 2x + 1$

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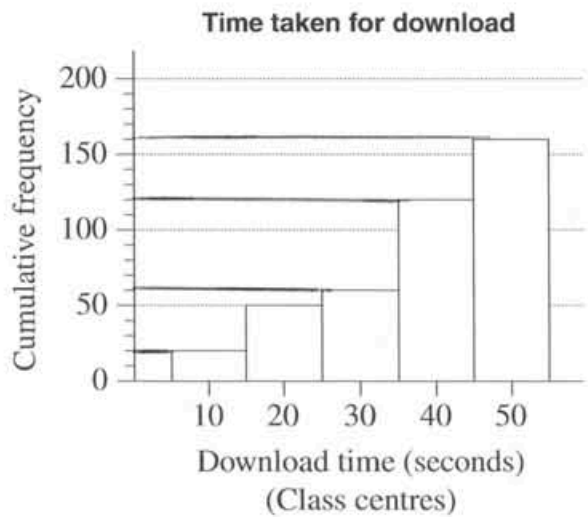


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- (e) The times taken for 160 music downloads were recorded, grouped into classes and then displayed using the cumulative frequency histogram shown. 2



On the diagram, draw the lines that are needed to find the median download time.

**Question 26 continues on page 16**

Question 26 (continued)

- (f) The weight of an object on the moon varies directly with its weight on Earth. 2  
An astronaut who weighs 84 kg on Earth weighs only 14 kg on the moon.

A lunar landing craft weighs 2449 kg when on the moon. Calculate the weight of this landing craft when on Earth.

astronaut Earth =  $14 + 70 = 84$

Moon =  $14 + 70 = 84$

Lunar landing craft =  $2449 - 700 = 1749 \text{ kg}$

Question 26 continues on page 17

Question 26 (continued)

- (g) Singapore is located at  $1^{\circ}\text{N } 104^{\circ}\text{E}$  and Sydney is located at  $34^{\circ}\text{S } 151^{\circ}\text{E}$ . 2

What is the time difference between Singapore and Sydney? (Ignore daylight saving.)

Singapore at  $1^{\circ}\text{N } 104^{\circ}\text{E}$   
 Sydney at  $34^{\circ}\text{S } 151^{\circ}\text{E}$

Time Difference is 4 hours earlier

**End of Question 26**

**Please turn over**

**Question 27** (15 marks)

- (a) Alex is buying a used car which has a sale price of \$13 380. In addition to the sale price there are the following costs:

Transfer of registration	\$30
Stamp Duty	.....

- (i) Stamp Duty for this car is calculated at \$3 for every \$100, or part thereof, of the sale price. 1

Calculate the Stamp Duty payable.

$$\begin{array}{r}
 13380 \div 100 \\
 \hline
 = 133.8
 \end{array}
 \qquad
 \begin{array}{r}
 133.8 \div 3 \\
 \hline
 = \$44.6 \\
 \hline
 = \$45 \text{ Stamp Duty}
 \end{array}$$

- (ii) Alex borrows the total amount to be paid for the car including Stamp Duty and transfer of registration. Interest on the loan is charged at a flat rate of 7.5% per annum. The loan is to be repaid in equal monthly instalments over 3 years. 4

Calculate Alex's monthly repayments.

~~$$\begin{array}{r}
 13380 + 30 + 45 \\
 \hline
 = 13455
 \end{array}$$~~

$$\begin{array}{r}
 13380 + 30 + 45 \\
 \hline
 = 13455
 \end{array}$$
~~$$\begin{array}{r}
 13455 \times 1.075^3 \\
 \hline
 = 1590.36 \\
 \hline
 \text{1590.36 months}
 \end{array}$$~~

$$\begin{array}{r}
 13455 \times 52 \times 7.5\% \\
 \hline
 = \$295 \text{ a month}
 \end{array}$$

**Question 27 continues on page 19**



Question 27 (continued)

- (iii) Alex wishes to take out comprehensive insurance for the car for 12 months. The cost of comprehensive insurance is calculated using the following: 3

Base rate	\$845
Fire Service Levy (FSL)	1% of base rate
Stamp Duty	5.5% of the total of base rate and FSL
GST	10% of the total of base rate and FSL

Find the total amount that Alex will need to pay for comprehensive insurance.

~~\$845 + 1% + 5.5% + 10%~~  
~~1 + 5.5 + 10% = 16.5%~~  
~~16.5% = 0.165~~  
~~100%~~  
~~\$845 + 0.165 =~~  
~~= \$845.165~~

- (iv) Alex has decided he will take out the comprehensive car insurance rather than the less expensive non-compulsory third-party car insurance. 1

What extra cover is provided by the comprehensive car insurance?

fire Service levy - 1% of base rate  
 Stamp Duty - 5.5% of base rate + FSL  
 GST - 10% of total base rate and FSL  
 10% + 5.5% + 1% = 16.5%

Question 27 continues on page 20

Question 27 (continued)

- (b) Xuso is comparing the costs of two different ways of travelling to university. 2

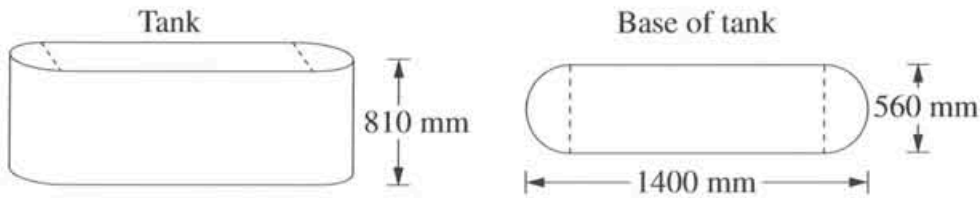
Xuso's motorcycle uses one litre of fuel for every 17 km travelled. The cost of fuel is \$1.67/L and the distance from her home to the university car park is 34 km. The cost of travelling by bus is \$36.40 for 10 single trips.

Which way of travelling is cheaper and by how much? Support your answer with calculations.

~~Motorbike = \$1.67 x 17 = \$28.39~~ / Motorcycle  
~~\$1.67 x 32 =~~  
 Bus = 10 trips = \$36.40  
~~36.40 ÷ 10 = 3.64~~  
 1 litre for 17 km  
 17 + 17 = 34 km  
 cost of fuel = 1.67 + 1.67 = \$3.34

- (c) The base of a water tank is in the shape of a rectangle with a semicircle at each end, as shown. 4

The tank is 1400 mm long, 560 mm wide, and has a height of 810 mm.



NOT TO SCALE

What is the capacity of the tank, to the nearest litre?

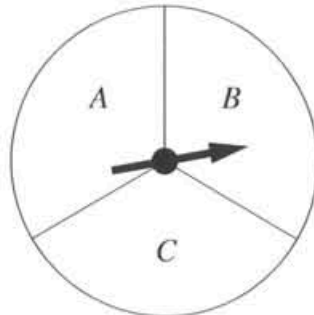
$1400 \times 560 \times 810$   
 $= 635L$

End of Question 27



Question 28 (15 marks)

- (a) James plays a game involving a spinner with sectors of equal size labelled A, B and C, as shown. 2



He pays \$2 to play the game. He wins \$5 if the spinner stops in A and 50 cents if it stops in B or C.

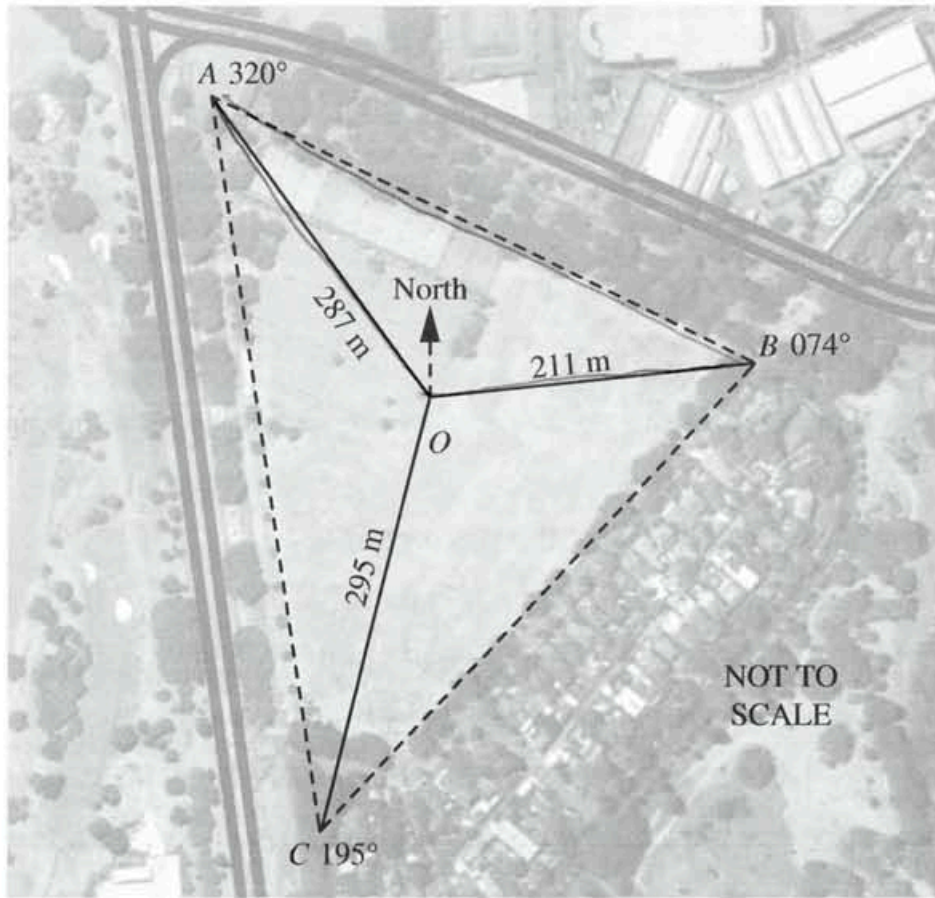
Calculate James's financial expectation for the game.

Pays \$2 - wins \$5 if stopped on A  
 - 50c if stopped on B & C  
 James will win no matter what  
 $\$2 + \$5 = \$7$  - stopped on A -  $\$2 = 5$  dollars  
 $\$2 + 50c = 2.50$  if stopped on B & C -  $\$2 = 50c$

Question 28 continues on page 22

Question 28 (continued)

(b) A radial compass survey of a sports centre is shown in the diagram.



(i) Show that the size of angle  $AOB$  is  $114^\circ$ .

1

.....  
 .....

Question 28 continues on page 23

Question 28 (continued)

(ii) Calculate the length of the boundary AB, to the nearest metre.

2

$$211 + 287$$


---


$$= 498$$


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$$= 500 \text{ m}$$


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(iii) Find the area of triangle AOB in hectares, correct to two significant figures.

3

~~82287~~

$$A = \frac{1}{2} ab \sin c$$


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$$A = \frac{1}{2} 320^\circ \times 074^\circ \sin 498$$


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$$A = 15845.016$$


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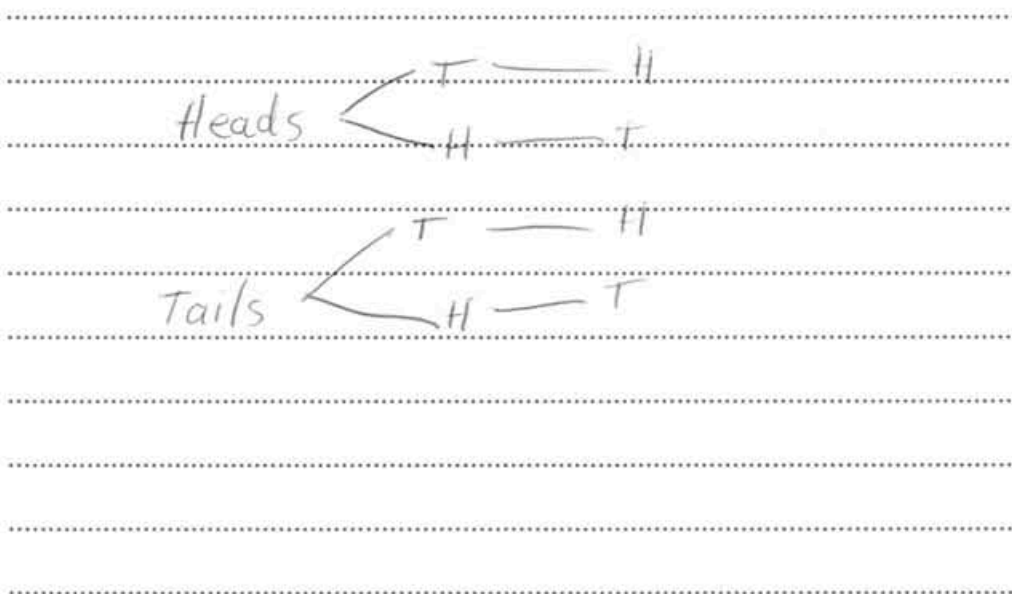
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(c) A fair coin is tossed three times. Using a tree diagram, or otherwise, calculate the probability of obtaining two heads and a tail in any order.

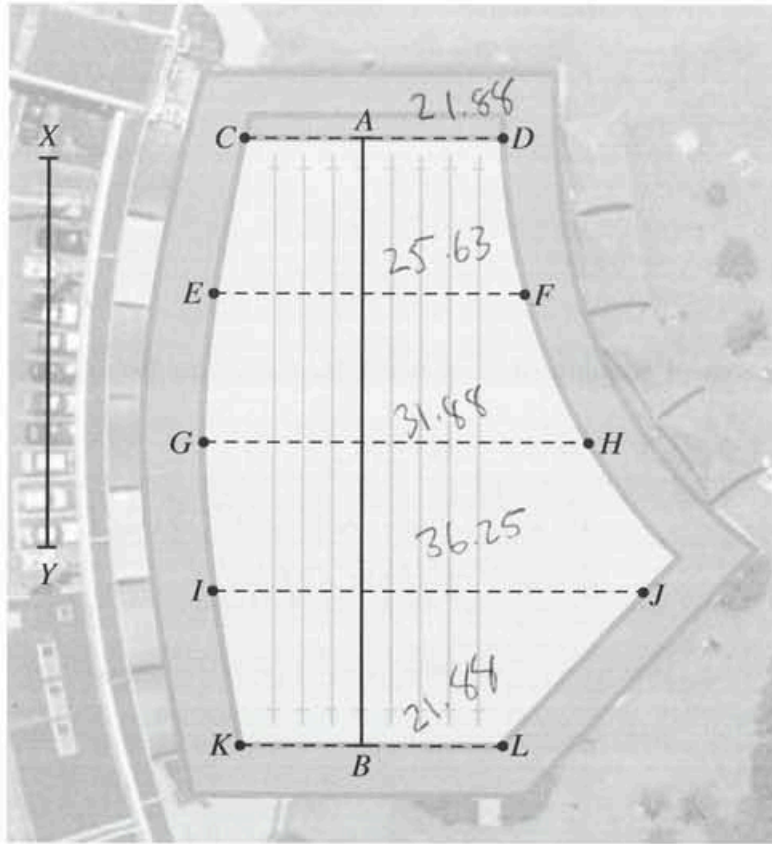
2



Question 28 continues on page 24

Question 28 (continued)

(d) An aerial diagram of a swimming pool is shown.



The swimming pool is a standard length of 50 metres but is not in the shape of a rectangle.

(i) By measuring the length  $AB$ , determine the scale of the diagram.

1

Scale = every 2cm = 20m

$1 \text{ cm} = 10 \text{ m}$

(ii) Using this scale, calculate the length  $XY$  of the car park, in metres.

1

50m

Question 28 continues on page 25

Question 28 (continued)

- (iii) In the diagram of the swimming pool, the five widths are measured to be: 3

$$CD = 21.88 \text{ m}$$

$$EF = 25.63 \text{ m}$$

$$GH = 31.88 \text{ m}$$

$$IJ = 36.25 \text{ m}$$

$$KL = 21.88 \text{ m}$$

The average depth of the pool is 1.2 m.

Calculate the approximate volume of the swimming pool, in cubic metres. In your calculations, use TWO applications of Simpson's Rule.

*Handwritten work:*

$$21.88 \times 25.63 = 560.7844$$

$$21.88 \times 36.25 \times 31.88 = 25285.622$$

$$25285.622 + 560.7844 = 25846.4064 \text{ m}^3$$

**End of Question 28**



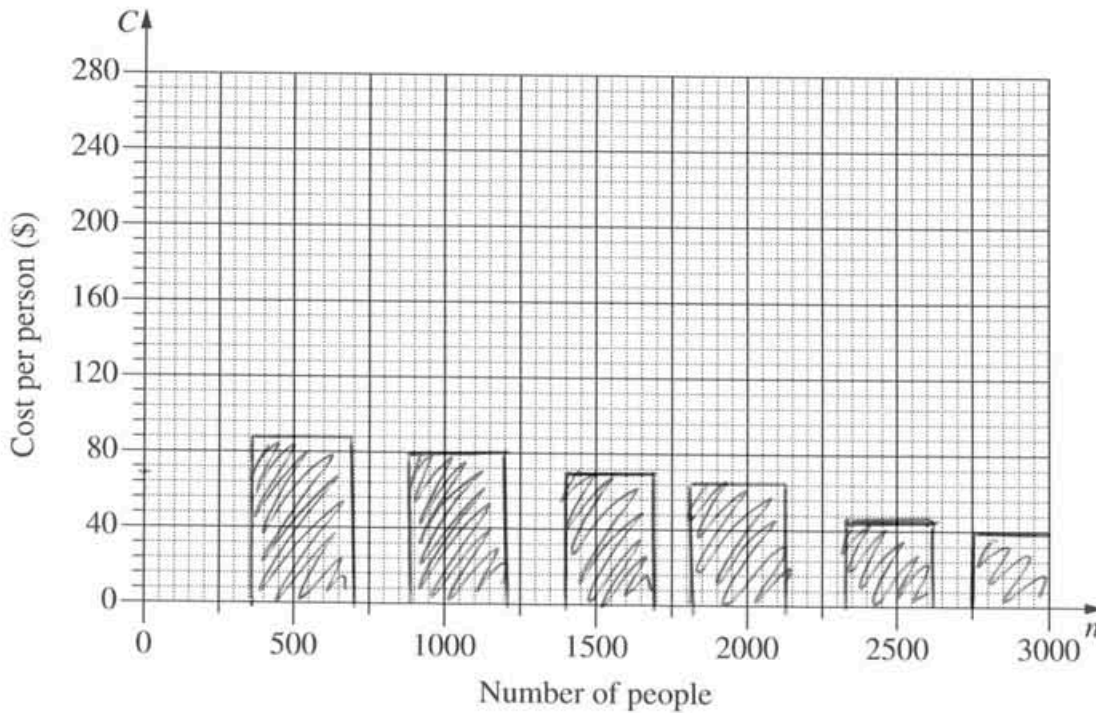
**Question 29** (15 marks)

- (a) The cost of hiring an open space for a music festival is \$120 000. The cost will be shared equally by the people attending the festival, so that  $C$  (in dollars) is the cost per person when  $n$  people attend the festival.

- (i) Complete the table below by filling in the THREE missing values. 1

Number of people ( $n$ )	500	1000	1500	2000	2500	3000
Cost per person ( $C$ )	88	80	68	60	48	40

- (ii) Using the values from the table, draw the graph showing the relationship between  $n$  and  $C$ . 2



- (iii) What equation represents the relationship between  $n$  and  $C$ ? 1

Every 1000 goes down by 20  
 $C = \frac{120000}{n}$

**Question 29 continues on page 27**

Question 29 (continued)

- (iv) Give ONE limitation of this equation in relation to this context. 1

.....  
 .....  
 .....

- (v) Is it possible for the cost per person to be \$94? Support your answer with appropriate calculations. 1

Yes  
 .....  
 .....  
 .....  
 .....

- (b) What is the maximum number of standard drinks that a male weighing 84 kg can consume over 4 hours in order to maintain a blood alcohol content (BAC) of less than 0.05? 3

.....  

$$\text{BAC}_{\text{male}} = \frac{10N - 7.5H}{6.8M}$$
 .....  

$$\text{BAC}_{\text{male}} = \frac{10^3 - 7.5 \times 4}{6.8 \times 84}$$
 .....  

$$= 3 \text{ standard drinks}$$
 .....  
 .....  
 .....

Question 29 continues on page 28

Question 29 (continued)

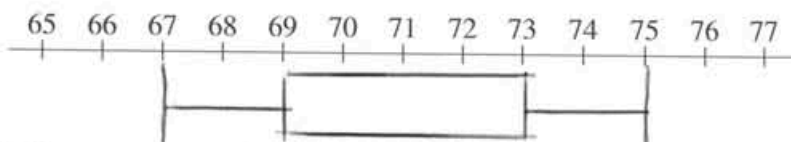
(c) Terry and Kim each sat twenty class tests. Terry's results on the tests are displayed in the box-and-whisker plot shown in part (i).

(i) Kim's 5-number summary for the tests is 67, 69, 71, 73, 75. 1

Draw a box-and-whisker plot to display Kim's results below that of Terry's results.



Kim



(ii) What percentage of Terry's results were below 69? 1

30%.

(iii) Terry claims that his results were better than Kim's. Is he correct? Justify your answer by referring to the summary statistics and the skewness of the distributions. 4

Maybe because

Yes, because Terry's box-and-whisker plot is larger than Kim's, and continues down the line to 76 as Terry's finishes at 73 whereas Kim's finishes at 75. Giving Terry a higher result of 76.

End of Question 29

**Question 30** (15 marks)

- (a) Chandra and Sascha plan to have \$20 000 in an investment account in 15 years time for their grandchild's university fees. 3

The interest rate for the investment account will be fixed at 3% per annum compounded monthly.

Calculate the amount that they will need to deposit into the account now in order to achieve their plan.

.....  

$$\frac{\$20\,000}{1.03^{15}}$$

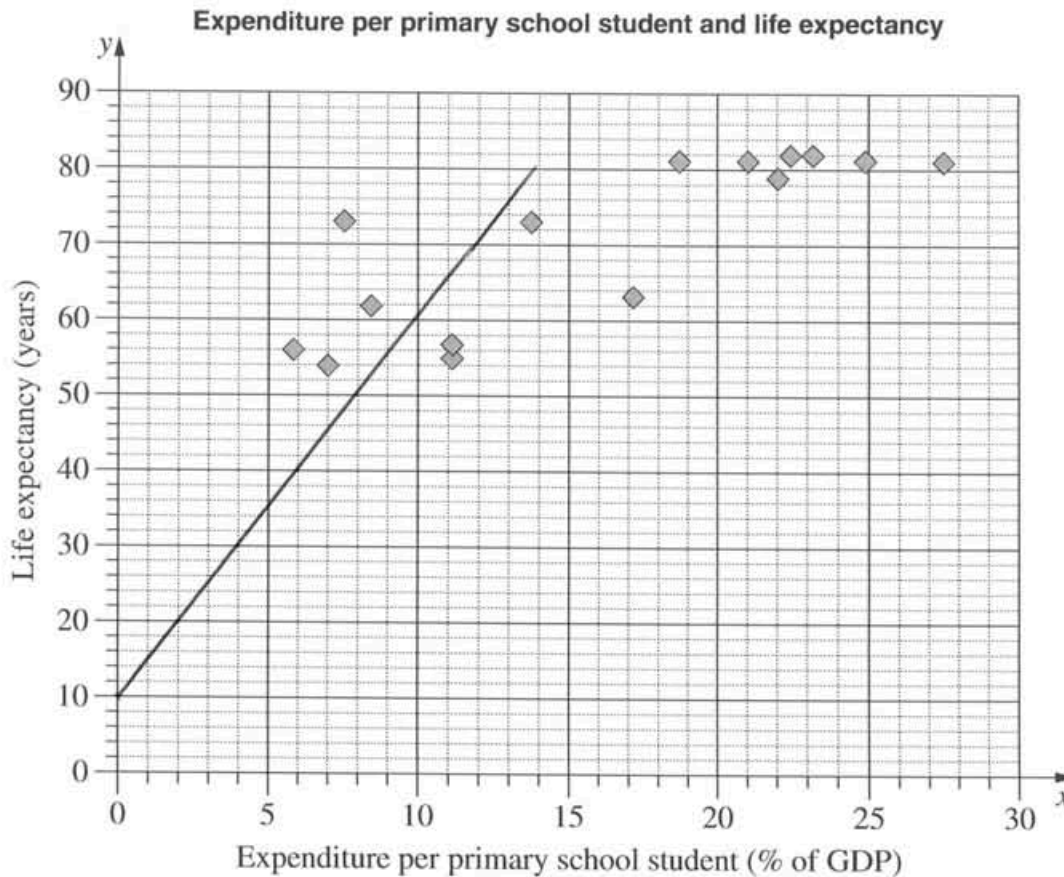
$$= \$897$$
.....  
.....  
.....  
.....  
.....

**Question 30 continues on page 30**



Question 30 (continued)

- (b) The scatterplot shows the relationship between expenditure per primary school student, as a percentage of a country's Gross Domestic Product (GDP), and the life expectancy in years for 15 countries.



- (i) For the given data, the correlation coefficient,  $r$ , is 0.83. What does this indicate about the relationship between expenditure per primary school student and life expectancy for the 15 countries?

1

*Life expectancy is rising.*

Question 30 continues on page 31



Question 30 (continued)

- (ii) For the data representing expenditure per primary school student,  $Q_L$  is 8.4 and  $Q_U$  is 22.5. 1

What is the interquartile range?

9.97  
.....  
.....

- (iii) Another country has an expenditure per primary school student of 47.6% of its GDP. Would this country be an outlier for this set of data? Justify your answer with calculations. 2

.....  
.....  
.....  
.....

- (iv) The expenditures per primary school student for the 15 countries in the scatterplot are: 2

5.9, 7, 7.6, 8.4, 11.2, 11.2, 13.7, 17.1, 18.7, 21.1, 22, 22.5, 23.2, 24.9, 27.6

Complete the table below by calculating the mean,  $\bar{x}$ , and the standard deviation,  $\sigma_x$ , of these data. Calculate both values to two decimal places.

The table also shows the mean,  $\bar{y}$ , and the standard deviation,  $\sigma_y$ , of life expectancy for the same 15 countries.

	Mean	Standard deviation
Expenditure per primary school student	$\bar{x} = 15.3$	$\sigma_x = 7.27$
Life expectancy	$\bar{y} = 70.73$	$\sigma_y = 10.94$

Question 30 continues on page 32

Question 30 (continued)

- (v) Using the values from the table in part (iv), show that the equation of the least-squares line of best fit is 2

$$y = 1.29x + 49.9.$$

Expenditure  
primary  
Student

mean =  $\bar{x} = 15.3$

standard deviation =  $\sqrt{120.73} \approx 10.99$

Life expectancy

mean =  $\bar{y} = 70.73$

standard deviation =  $\sqrt{119.4} \approx 10.93$

- (vi) On the scatterplot on page 30, draw the least-squares line of best fit,  $y = 1.29x + 49.9$ . 2

- (vii) Using this line, or otherwise, estimate the life expectancy in a country which has an expenditure per primary school student of 18% of its GDP. 1

60.2

- (viii) Why is this line NOT useful for predicting life expectancy in a country which has expenditure per primary school student of 60% of its GDP? 1

~~Students~~ The line does not target 60% of primary school students.

**End of paper**





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