2014 HIGHER SCHOOL CERTIFICATE EXAMINATION Mathematics General 2

Section II

75 marks Attempt Questions 26–30 Allow about 1 hour and 55 minutes for this section

Answer the questions in the spaces provided.

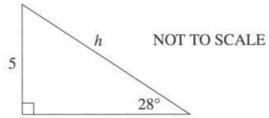
Your responses should include relevant mathematical reasoning and/or calculations.

Extra writing space is provided on pages 33 and 34. If you use this space, clearly indicate which question you are answering.

Please turn over

Question 26 (15 marks)

- (a) Expand $4x(7x^4 x^2)$.
- Calculate the value of h correct to two decimal places. 2



Solve the equation $\frac{5x+1}{3} - 4 = 5 - 7x$. 3

Question 26 continues on page 15

2

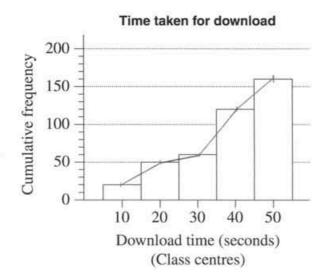
Question 26 (continued)

(d) Solve these simultaneous equations to find the values of x and y.

y = 2x + 1 x - 2y - 4 = 0 x - 2y - 4 = 0

x - 4x - 2 - 4 = 0 y = -4 = 3-3x - 6 = 6 y = -3

(e) The times taken for 160 music downloads were recorded, grouped into classes and then displayed using the cumulative frequency histogram shown.



On the diagram, draw the lines that are needed to find the median download time.

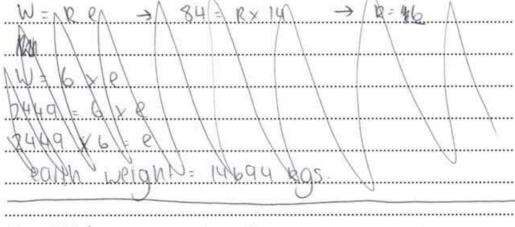
Question 26 continues on page 16

Question 26 (continued)

w' ·

(f) The weight of an object on the moon varies directly with its weight on Earth. An astronaut who weighs 84 kg on Earth weighs only 14 kg on the moon.

A lunar landing craft weighs 2449 kg when on the moon. Calculate the weight of this landing craft when on Earth.



e = RW	→ 84 = R × 14 → R = 6
mach	e= 6 x w
	P= 6 x 2449

e = 14694 kgs

Question 26 continues on page 17

Question 26 (continued)

Questions 26-30

(g) Singapore is located at 1°N 104°E and Sydney is located at 34°S 151°E.

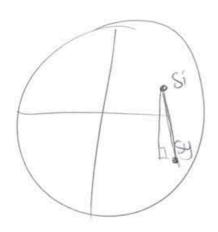
2

What is the time difference between Singapore and Sydney? (Ignore daylight saving.)

10 - 11 100 100	
10 = 4 MIV	

				********	***************************************	
(#	110	FINAD	difference	15	THOMAIN	
	1014	711111)	1901000	

End of Question 26



Please turn over

0		27	115	
Quesi	non	21	(1)	marks)

(a)	Alex is buying a used car which has a sale price of \$13 380. In addition to the
	sale price there are the following costs:

Transfer of registration \$30 Stamp Duty

(i)	Stamp Duty for this car is calculated at \$3 for every \$100, or part thereof,
	of the sale price.

1

Calculate the Stamp Duty payable.

SOIR DYICR = \$ W	NAMA - 100
= \$VBALNIVO × 3	= BNADRABAR SYOLYO
	= NAMORMBOR \$ 401. 40
	2 3 2 33

(ii) Alex borrows the total amount to be paid for the car including Stamp Duty and transfer of registration. Interest on the loan is charged at a flat rate of 7.5% per annum. The loan is to be repaid in equal monthly instalments over 3 years.

Calculate Alex's monthly repayments.

10101 amount = \$13811-40
N38N48×12075×3
= 13811-40 × 0-075 × 3M
= 3 BM/04/04/MM 3107-57
\$13811-40+\$3107-57 = \$16918-97
1698-97=36 = \$469.97
: MONTHLY PRYMENTS

Question 27 continues on page 19

Question 27 (continued)

(iii)		comprehensive insurance for the car for prehensive insurance is calculated using the	3
	Base rate	\$845	
	Fire Service Levy (FSL)	1% of base rate	
	Stamp Duty	5.5% of the total of base rate and FSL	
	GST	10% of the total of base rate and FSL.	
	Find the total amount that insurance.	Alex will need to pay for comprehensive	
	BR = 845		
		5 = \$8.45 → TOTAL = \$853.45	
	SD = 5.50 10 x 85	3.45 = \$46.94	
	UST = 10°10 x 853	45 = \$85-35	
	W.	45 + 8.45 + 46.94 + 85.35 985.74	
(iv)		e out the comprehensive car insurance rather compulsory third-party car insurance.	1
	What extra cover is provide	d by the comprehensive car insurance?	
	compilinensive	cal insurance provides	
	coner, for nome	cal, your passanges.	

Question 27 continues on page 20

Question 27 (continued)

(b) Xuso is comparing the costs of two different ways of travelling to university.

2

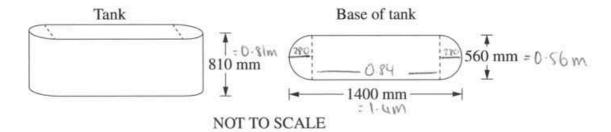
Xuso's motorcycle uses one litre of fuel for every 17 km travelled. The cost of fuel is \$1.67/L and the distance from her home to the university car park is 34 km. The cost of travelling by bus is \$36.40 for 10 single trips.

Which way of travelling is cheaper and by how much? Support your answer with calculations.

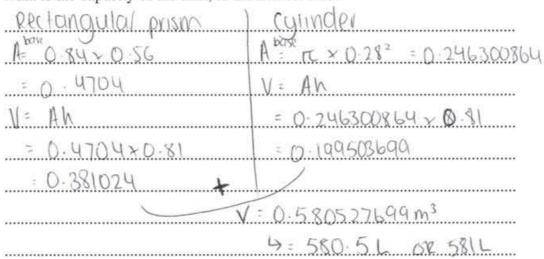
MotorCycle	l but
34: 17: 2 → 21 of	\$36.40 (01 10 1110)
PEHO1 = (167×2)=\$3.34.	1
per hip & \$33.40 lu	
10 tribs	
: motorcycle	lis cheaper for 10 hips

(c) The base of a water tank is in the shape of a rectangle with a semicircle at each end, as shown.

The tank is 1400 mm long, 560 mm wide, and has a height of 810 mm.



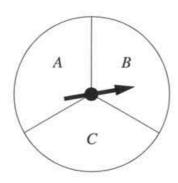
What is the capacity of the tank, to the nearest litre?



End of Question 27

Question 28 (15 marks)

(a) James plays a game involving a spinner with sectors of equal size labelled A, B and C, as shown.



He pays \$2 to play the game. He wins \$5 if the spinner stops in A and 50 cents if it stops in B or C.

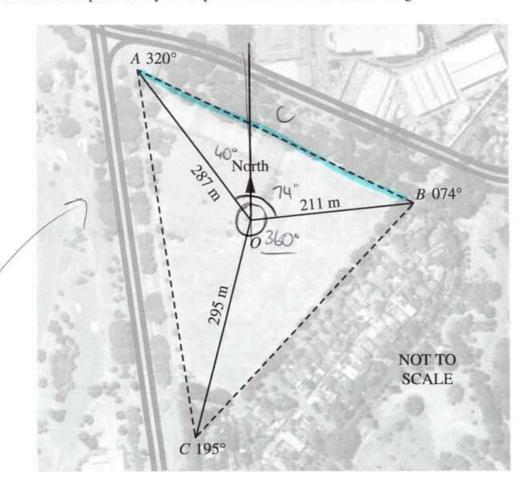
Calculate James's financial expectation for the game.

BILLY	(!	0 X 3) 1 (0.5x	<u>-3.)</u> .			
= 2								
	ŢĮ.	ıĮ.	costs	82	Ю	pla	u a m	P
financ	101	0 18	ecta no	V =	8	1 ()	
NB	15	ξX,	DECKQ	Ю	'nΛ	eak	even	
			, po.)					

Question 28 continues on page 22

Question 28 (continued)

(b) A radial compass survey of a sports centre is shown in the diagram.



(i) Show that the size of angle AOB is 114°.

As B is D74° # A is 320°

A is 40° away from north (from sputh)

and B is 74° away

74+40 = 114 -> making LAOB 114°

Question 28 (continued)

(ii) Calculate the length of the boundary AB, to the nearest metre.

2

C = Jarb - 2ab COSC C = J(297+211) - 2(287×211)×COS114° C = 223.07 2. boundary AB = 223m

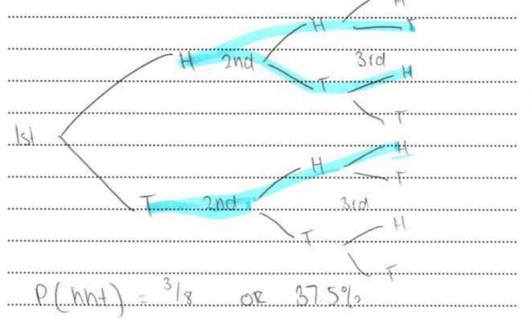
(iii) Find the area of triangle AOB in hectares, correct to two significant figures.

3

A= $\frac{1}{2}$ ah sin C = $\frac{1}{2}$ (287+211) sin 114° = 227. 472819 = 227. 47 m² 1 ha = 10000 m² \rightarrow 227. 47:10000 A= 0.023 ha

(c) A fair coin is tossed three times. Using a tree diagram, or otherwise, calculate the probability of obtaining two heads and a tail in any order.

2

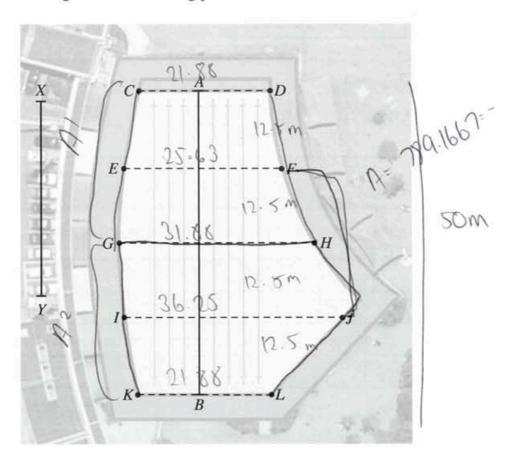


(2)

Question 28 continues on page 24

Question 28 (continued)

(d) An aerial diagram of a swimming pool is shown.



The swimming pool is a standard length of 50 metres but is not in the shape of a rectangle.

(i) By measuring the length AB, determine the scale of the diagram. 1 AB = 50 m - d10010 m = 800 m

50 : X = 6.25 m

1 cm = 6.75 m

(ii) Using this scale, calculate the length XY of the car park, in metres.

5-1 x 6-25 = 31-875 : length car pack = 32m

Question 28 continues on page 25

Question 28 (continued)

(iii) In the diagram of the swimming pool, the five widths are measured to be:

CD = 21.88 m

EF = 25.63 m

GH = 31.88 m

IJ = 36.25 m

KL = 21.88 m

The average depth of the pool is 1.2 m.

Calculate the approximate volume of the swimming pool, in cubic metres. In your calculations, use TWO applications of Simpson's Rule.

A' = 3 (21.88 + (4x2x 63)+3188	Nolume
A' = 650 - 833 - m ²	V= 12-8 (650-83+ (41789.167) , 828-16
A2= 3 (31.88+(4×36.25).21-81)	V= 19,313-19167m3
Az: 528.167 mz	
	volume
	= 19313.20 ms
A .	

End of Question 28

Question 29 (15 marks)

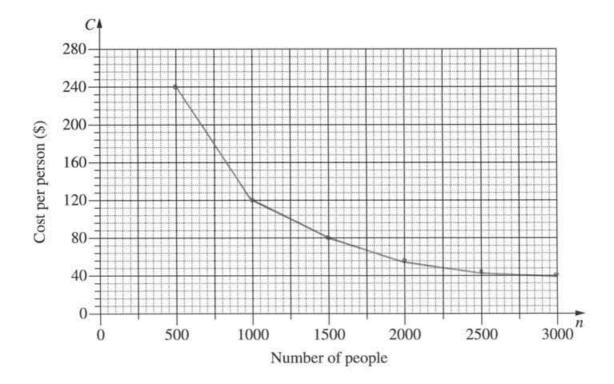
- (a) The cost of hiring an open space for a music festival is \$120 000. The cost will be shared equally by the people attending the festival, so that C (in dollars) is the cost per person when n people attend the festival.
 - (i) Complete the table below by filling in the THREE missing values.

-	

Number of people (n)	500	1000	1500	2000	2500	3000
Cost per person (C)	240	120	80	60	48	40

(ii) Using the values from the table, draw the graph showing the relationship between n and C.

2



(iii) What equation represents the relationship between n and C?

1

Question 29 continues on page 27

(b)

Question 29 (continued)

(iv)	Give ONE limitation of this equation in relation to this context. 11 ONLY INCLUDES THE COST OF THE SAME	1
	hire, not the food drintes pands	
	INDUNCERS EXC	
(v)	Is it possible for the cost per person to be \$94? Support your answer with appropriate calculations.	1
	94 = 120000 (24)	
	94 n = 120000 (=94)	
	n= 1276-60	
	il is not possible, as it is a decimal,	
	and n' represents people a cannol be a	
	decimal.	
can co	is the maximum number of standard drinks that a <u>male</u> weighing <u>84 kg</u> onsume over <u>4 hou</u> rs in order to maintain a blood alcohol content (BAC) is than 0.05?	3
Λ Λ	C = 10N - 7.5H	
	6-8M	
X (JURSS: 6	
BA	C = 10(6) - 7.5(4)	
	6.8 (84)	
**********	= 0.052 → too high	
* (JUPS): 5	
BAL	(=10(5)-75(4)	
	6.8(84)	
*********	= 0.0350	
+ ,	Max of 5 standard drinks	
see the see	MAX OF 2 2000 (MOVIE).	

Question 29 continues on page 28

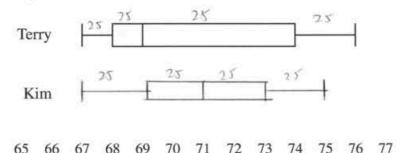
Question 29 (continued)

- (c) Terry and Kim each sat twenty class tests. Terry's results on the tests are displayed in the box-and-whisker plot shown in part (i).
 - (i) Kim's 5-number summary for the tests is 67, 69, 71, 73, 75.

1

4

Draw a box-and-whisker plot to display Kim's results below that of Terry's results.



- (ii) What percentage of Terry's results were below 69?
- (iii) Terry claims that his results were better than Kim's. Is he correct? Justify your answer by referring to the summary statistics and the skewness of the distributions.

Terry is incorrect, as;
1. his data is negativly sheved:
2 Only 50% of hes Hist scores
Were Thour 69, novever 75%
of kims test scores were above
69, evidently showing nel results
were better.
3 Although his highest store was
Maner than rims, the majority of
his were lower than hers.
" Kinns scores were better a terry is

End of Question 29

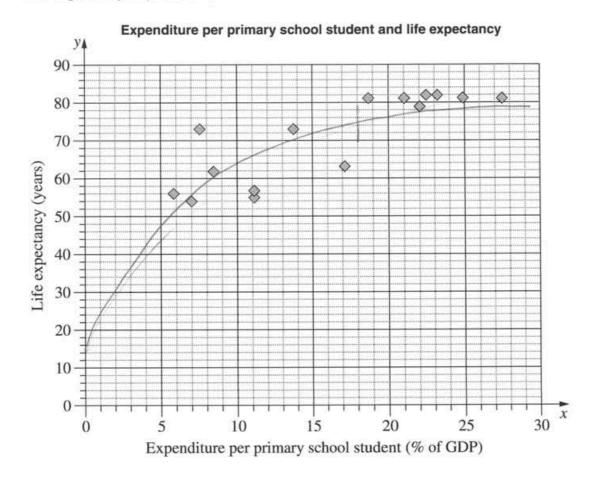
Question 30 (15 marks)

The interest rate for the investment account will be $\underline{\text{fixed at } 3\% \text{ per annum}}$ compounded monthly.
Calculate the amount that they will need to deposit into the account now in order to achieve their plan.
20000 in 15 yis, @ 0.0025 per mont
A = P(I+V)n
20000 = P (1+0.0025) 180
20000 = P x 1-567431725 (=1567481725)
12,759.73 = P
: They will need to deposit \$12759.73
to achieve their plan.

Question 30 continues on page 30

Question 30 (continued)

(b) The scatterplot shows the relationship between expenditure per primary school student, as a percentage of a country's Gross Domestic Product (GDP), and the life expectancy in years for 15 countries.



(i) For the given data, the correlation coefficient, r, is 0.83. What does this indicate about the relationship between expenditure per primary school student and life expectancy for the 15 countries?

is indicates a positive relationship as the higher the expenditure primary school student (10 of GDP) the higher the

Question 30 continues on page 31

Question 30 (continued)

(ii)	For the data representing expenditure per primary school student, Q_t is 8.4
	and Q_U is 22.5.

1

2

What is the interquartile range?

10:R)2.5	 8.4	 	 	 	 	,
=	1	4.1						

(iii) Another country has an expenditure per primary school student of 47.6% of its GDP. Would this country be an outlier for this set of data? Justify your answer with calculations.

Qu.	1.5 1	101	2 ->	27	5 * 1.5	2 14-1	
= 4	365						
	ues	H	is	an	outlier		
10000000000000	U	10:00:00:00					

(iv) The expenditures per primary school student for the 15 countries in the scatterplot are:

Complete the table below by calculating the mean, \bar{x} , and the standard deviation, σ_x , of these data. Calculate both values to two decimal places.

The table also shows the mean, \bar{y} , and the standard deviation, σ_y , of life expectancy for the same 15 countries.

	Mean	Standard deviation
Expenditure per primary school student	x =VALAM	$\sigma_{x} = 7.03$
Life expectancy	$\bar{y} = 70.73$	$\sigma_{y} = 10.94$

Question 30 continues on page 32

Question 30 (continued)

(v) Using the values from the table in part (iv), show that the equation of the least-squares line of best fit is

2

(v)	y = 1.29x + 49.9	9.	4. Intercelot
conelation	roefficient = 0.8	<u>g</u>	g fgradient x x
z : 16.1	y = 1.29x + 49.9 COREGIENT > 0 - 8		= 40 a
ū = 70.	73		=
gradient =	0.83 × 10.94 7.03	= 1-201	
u = 01a	dienl * x + y	intercept	
G= 1.20	2 1 49.9		
	12149915	the least	SCI LICU PS
	DRSF FIL.		

(vi) On the scatterplot on page 30, draw the least-squares line of best fit, y = 1.29x + 49.9.

1

1

(vii) Using this line, or otherwise, estimate the life expectancy in a country which has an expenditure per primary school student of 18% of its GDP.

BELWEEN 70 \$ 80.

SO 10UGNU 700 75 415.

(viii) Why is this line NOT useful for predicting life expectancy in a country which has expenditure per primary school student of 60% of its GDP?

nowever it becomes physically impossible.

The live to the age that the

······

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- 33 -

Section II extra writing space
If you use this space, clearly indicate which question you are answering.
- 34 -

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